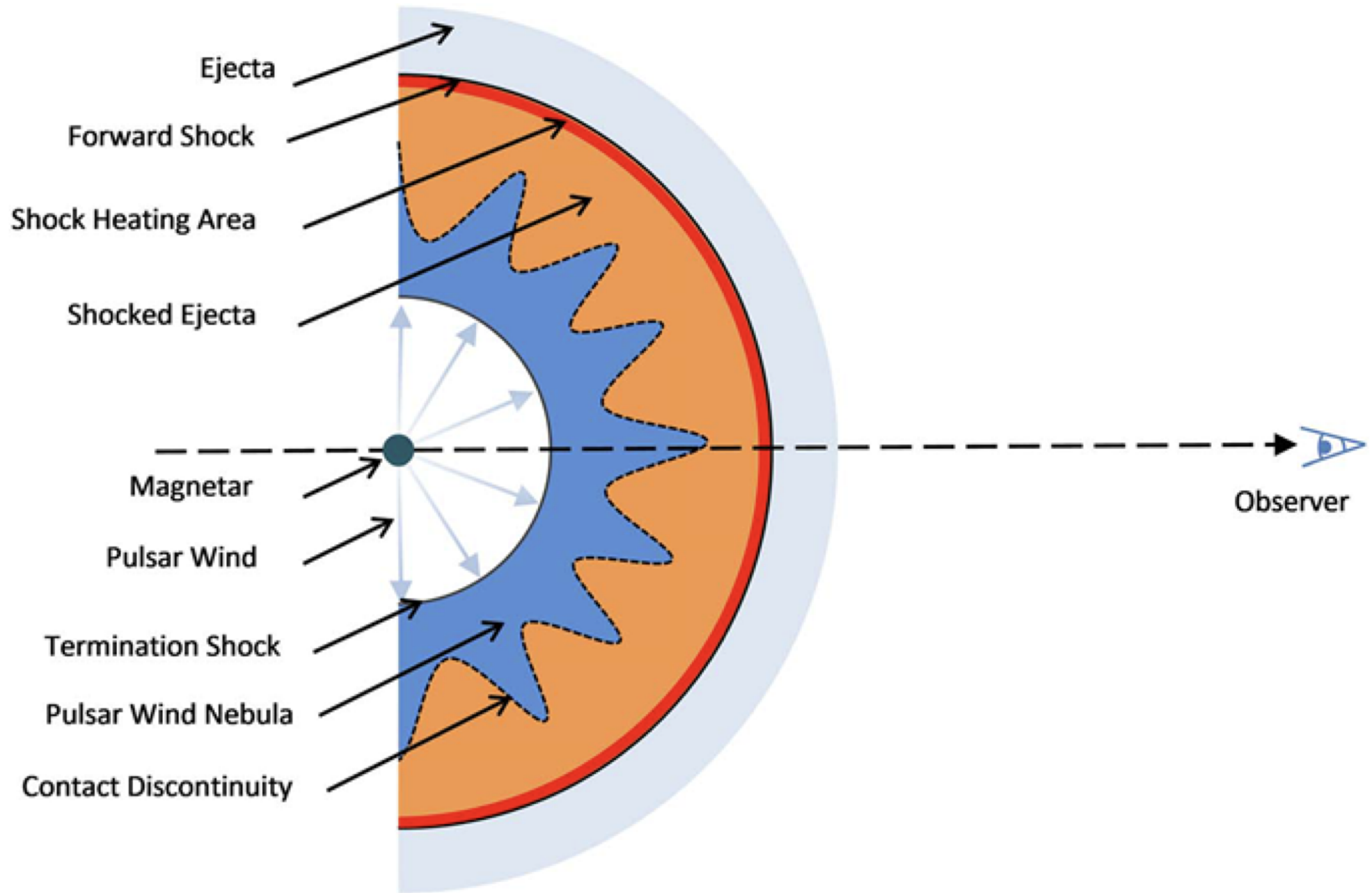


Magnetar Wind-Driven Shock Breakout Emission

Speaker: 金奕澄

2024.12.16

<http://dx.doi.org/10.3847/0004-637X/819/2/120>



Heating zone

- $\frac{dU_{heating}}{dt} = H_{sh} - P_{heating} \frac{d(V_{heating})}{dt} - L_{SBO}$
- $H_{sh} = \frac{1}{2} \left[v_{sh} - v_{ej}(r_{sh}, t) \right]^2 \frac{dM}{dt}$
- $\frac{L_{SBO}}{4\pi r_{sh}^2} = c \frac{\partial P_{heating}}{\partial \tau}, P_{heating} = \frac{U_{heating}}{3V_{heating}}$
- $V_{heating} = \epsilon V_{sh}$

Residual part

- $\frac{dU_{res}}{dt} = L_{inj} - P \frac{dV_{sh}}{dt} - L_{SN/MN},$
- $L_{inj} = L_{Ni\&Co} + L_{sd}$
- $\frac{L_{SN}}{4\pi r_{sh}^2} = c \frac{\partial P_{res}}{\partial \tau}$
- $V_{res} \approx V_{sh} = \frac{4\pi}{3} r_{sh}^3$

Energy injection

$$\bullet L_{sd} = L_{sd,0} \left(1 + \frac{t}{\tau_{sd}}\right)^{-2}$$

$$\bullet L_{sd,0} = \frac{B^2 R_{ns}^6 \Omega_0^4 \sin^2 \chi}{6c^3}$$

$$\bullet \tau_{sd} = \frac{6I_{ns}c^3}{B^2 R_{ns}^6 \Omega_0^2}$$

$$\bullet L_{NiCo} = L_{Ni} + L_{Co}$$

$$\bullet \frac{dN_{Ni}}{dt} = \lambda_{Ni} N_{Ni}$$

$$\bullet \frac{dN_{Co}}{dt} = \lambda_{Ni} N_{Ni} - \lambda_{Co} N_{Co}$$

$$\bullet N_{Ni} = N_0 e^{-\lambda_{Ni} t}$$

$$\bullet N_{Co} = \frac{\lambda_{Ni} N_0 (e^{-\lambda_{Ni} t} - e^{-\lambda_{Co} t})}{\lambda_{Co} - \lambda_{Ni}}$$

$$\bullet L = \lambda N(t) Q$$

Shock Dynamics

- Total energy of shocked region:

- $E = \frac{1}{2} M v_{sh}^2 + U \quad (1)$

- Total energy variation:

- $dE = (L_{inj} - L_{SBO} - L_{SN/MN})dt + \frac{1}{2} v_{ej}^2(r_{sh}, t)dM \quad (2)$

- $d(1)=(2) \implies \frac{dv_{sh}}{dt} = \frac{1}{Mv_{sh}} \left[(L_{inj} - L_{SBO} - L_{SN}) - \frac{1}{2} (v_{sh}^2 - v_{ej}^2) \frac{dM}{dt} - \frac{dU}{dt} \right]$

Density & Velocity Distribution

- (Nagakura et al. 2014)

$$\rho_{\text{ej}}(r, t) = \frac{(\delta - 3)M_{\text{ej}}}{4\pi r_{\text{max}}^3} \left[\left(\frac{r_{\text{min}}}{r_{\text{max}}} \right)^{3-\delta} - 1 \right]^{-1} \left(\frac{r}{r_{\text{max}}} \right)^{-\delta}, \quad (1)$$

and

$$v_{\text{ej}}(r, t) = v_{\text{max}} \frac{r}{r_{\text{max}}(t)}, \quad \text{for } r \leq r_{\text{max}}(t), \quad (2)$$

- $\delta: 3 \sim 4$

Result

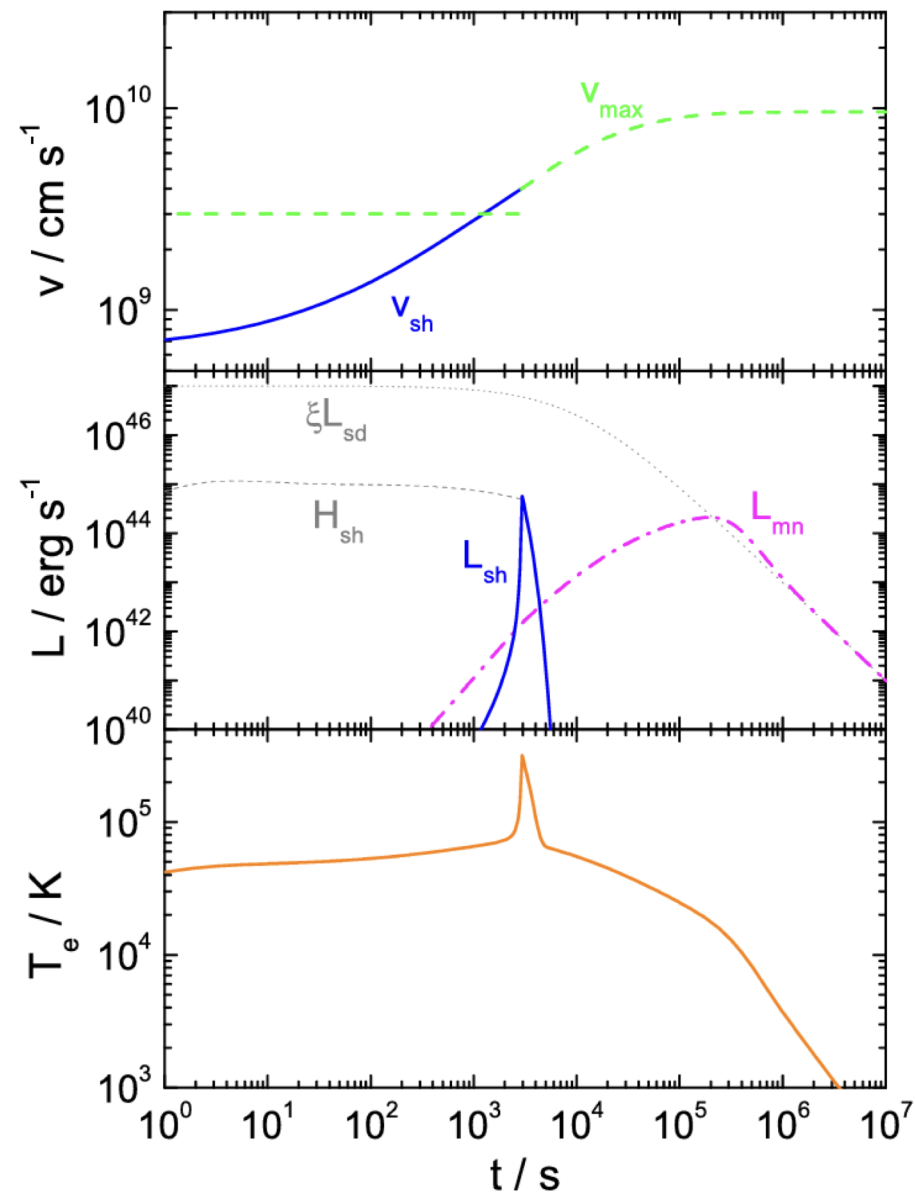


Figure 1. Evolutions of velocities (top), bolometric luminosities (middle), and emission temperature (bottom). In the middle panel, the injected spin-down luminosity (ξL_{sd}) and the shock heating rate (H_{sh}) are also presented for reference. The model parameters are taken as $\xi L_{\text{sd},i} = 10^{47} \text{ erg s}^{-1}$, $t_{\text{md}} = 10^4 \text{ s}$, $\Delta t = 2 \text{ s}$, $M_{\text{ej}} = 0.01 M_{\odot}$, $v_{\text{max}} = 0.1c$, $\delta = 3.5$, and $\kappa = 10 \text{ cm}^2 \text{ g}^{-1}$.

Blackbody Spectrum

- $T_{eff} = \left(\frac{L_{SBO} + L_{SN}}{4\pi r_{max}^2 \sigma} \right)^{1/4}$
- $\nu L_{\nu} = \frac{8\pi^2 r_{max}^2}{h^3 c^2} \frac{(h\nu)^4}{\exp\left(\frac{h\nu}{kT_{eff}}\right) - 1}$

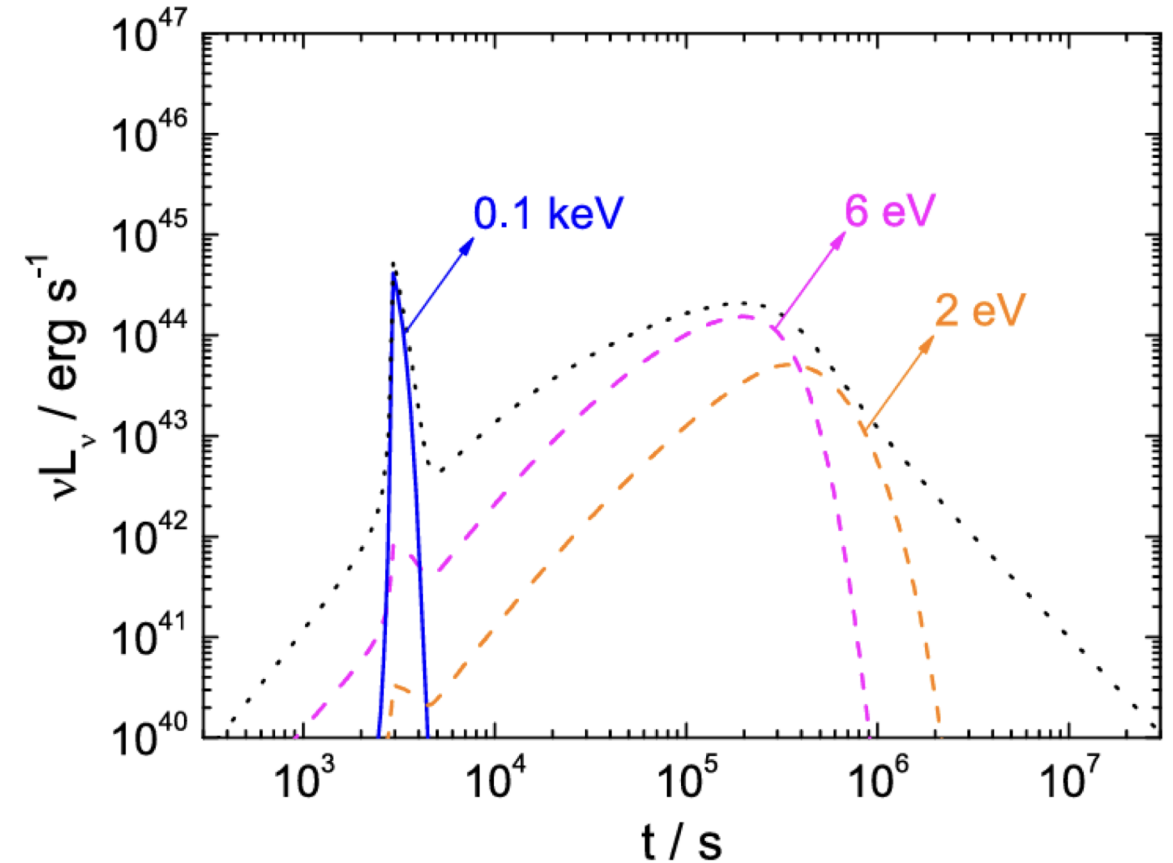
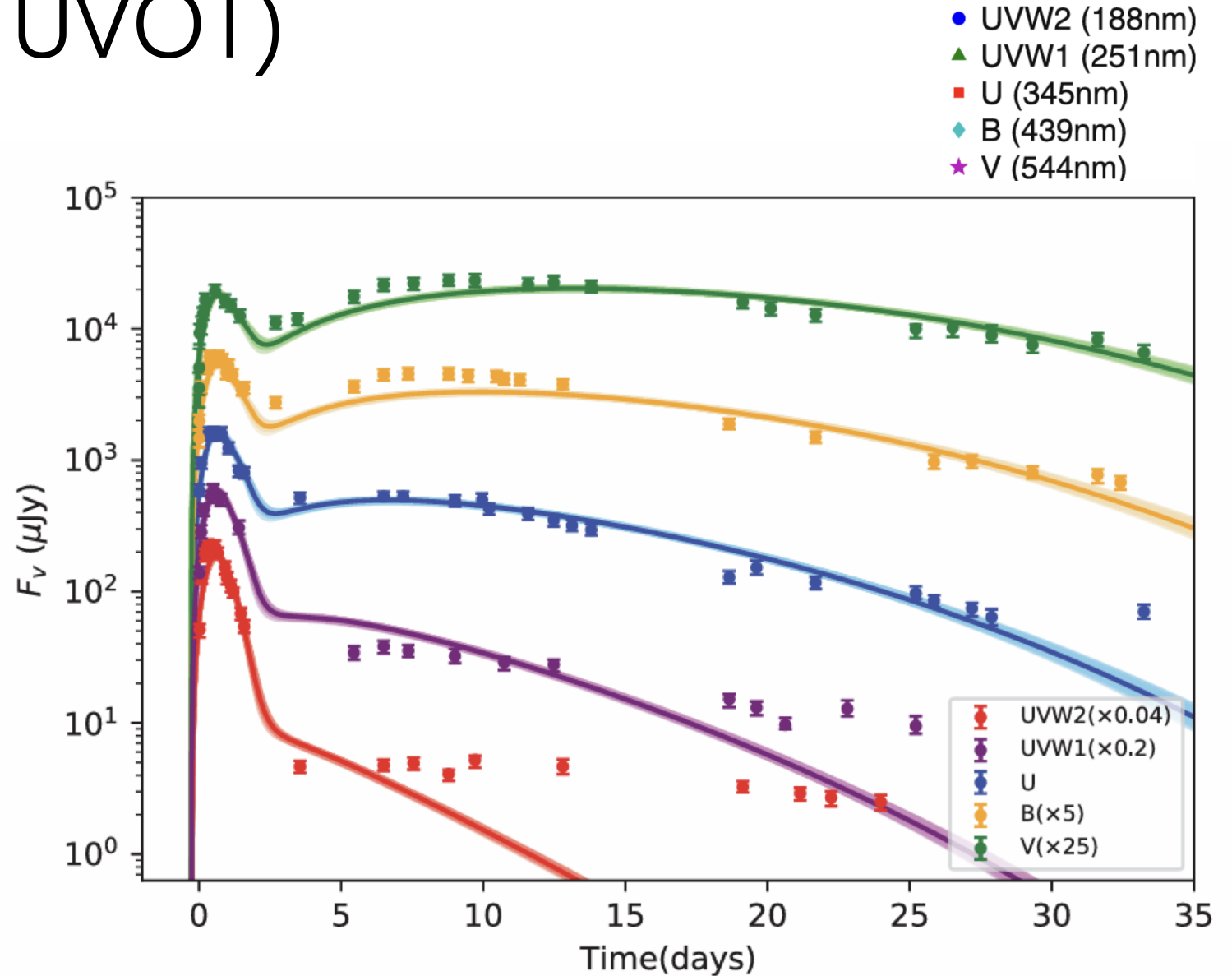


Figure 2. Three chromatic light curves for photon energies of $h\nu = 0.1$ keV (soft X-ray; solid), 6 eV (UV; dashed), and 2 eV (optical; dash-dotted), respectively, where the bolometric light curve (dotted) is presented as a reference.

SN 2006aj (Swift UVOT)

- (Density distribution:
Liu et al. 2018)



Conclusion

- Magnetar central engine could explain the light-curves of double-peak supernovae/mergernovae.
- The discovery of magnetar-powered transients could substantially modify and expand our conventional understandings of dynamics, radiation mechanism, and properties of newborn magnetars.

Thank you