



# Revealing Limitation in the Standard Cosmological Model: A Redshift-Dependent Hubble Constant from Fast Radio Bursts

**Subtitle: Is the Standard Model of Cosmology Truly “Standard”?**

Surajit Kalita , Akhil Uniyal , Tomasz Bulik ,and Yosuke Mizuno (arXiv:2506.14947)

Speaker: kongjun Zhang

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# Introduction

## Why Should We Care? The "Hubble Tension"

Hubble Tension: The discrepancy in the Hubble constant ( $H_0$ ) measured using two types of "cosmic rulers."

- Early-Universe (Planck18 CMB) eg.,  $(67.4 \pm 0.5) \text{ km s}^{-1}\text{Mpc}^{-1}$
- late-Universe (SH0ES distance-ladder) eg.,  $(73.04 \pm 1.04) \text{ km s}^{-1}\text{Mpc}^{-1}$

$\Lambda$ CDM assumption: Hubble constant  $H_0$  remains invariant across all redshifts.

### **Knowledge Gap**

Is this tension due to observational systematics? Or a fundamental problem with  $\Lambda$ CDM?

Need independent observational probes to test this

### **Core Research Question**

Is  $H_0$  truly constant across different redshifts? If not, this implies a fundamental inadequacy in the  $\Lambda$ CDM model.

# Data

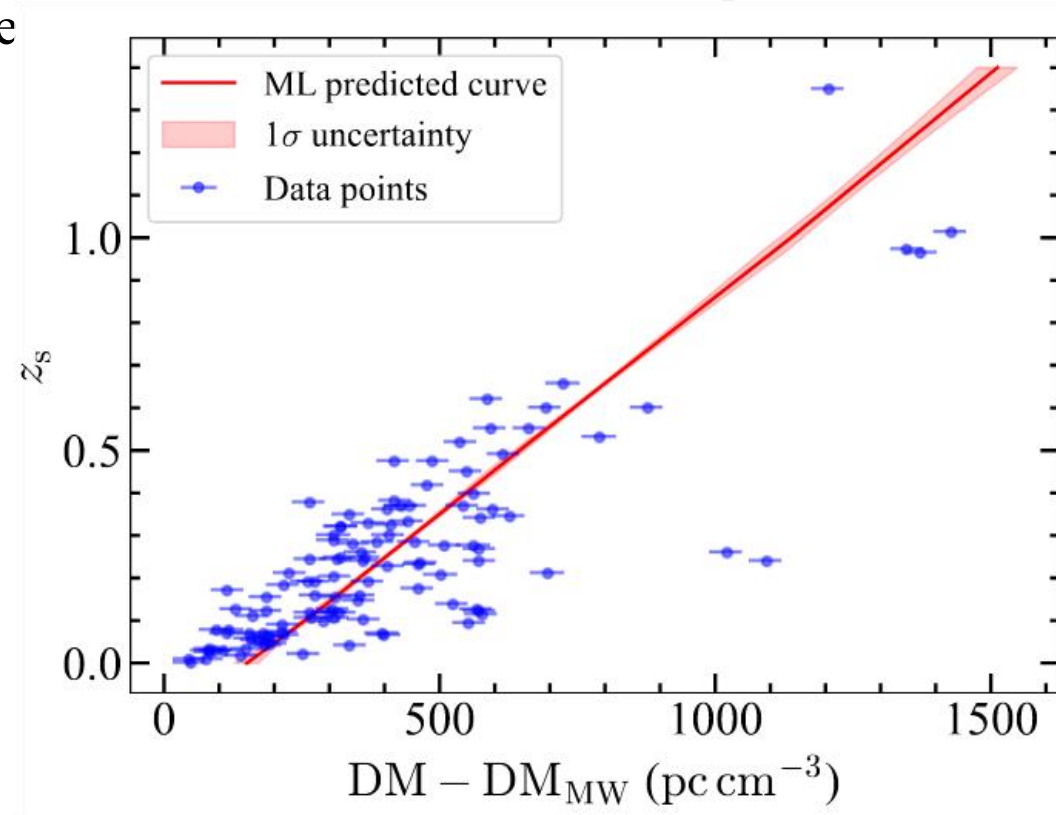
## Dataset

- 114 well-localized Fast Radio Bursts (FRBs)
- Redshift range:  $z \approx 0$  to  $z \approx 1.35$
- Exploiting the Dispersion Measure (DM) - redshift relation

## Data

### First Approach: Artificial Neural Network (ANN)

- Architecture: Input layer + 2 hidden layers (100 neurons each) + Output layer
- Training: Continuous reconstruction of  $DM' - z$  relationship
- Advantage: Captures fine

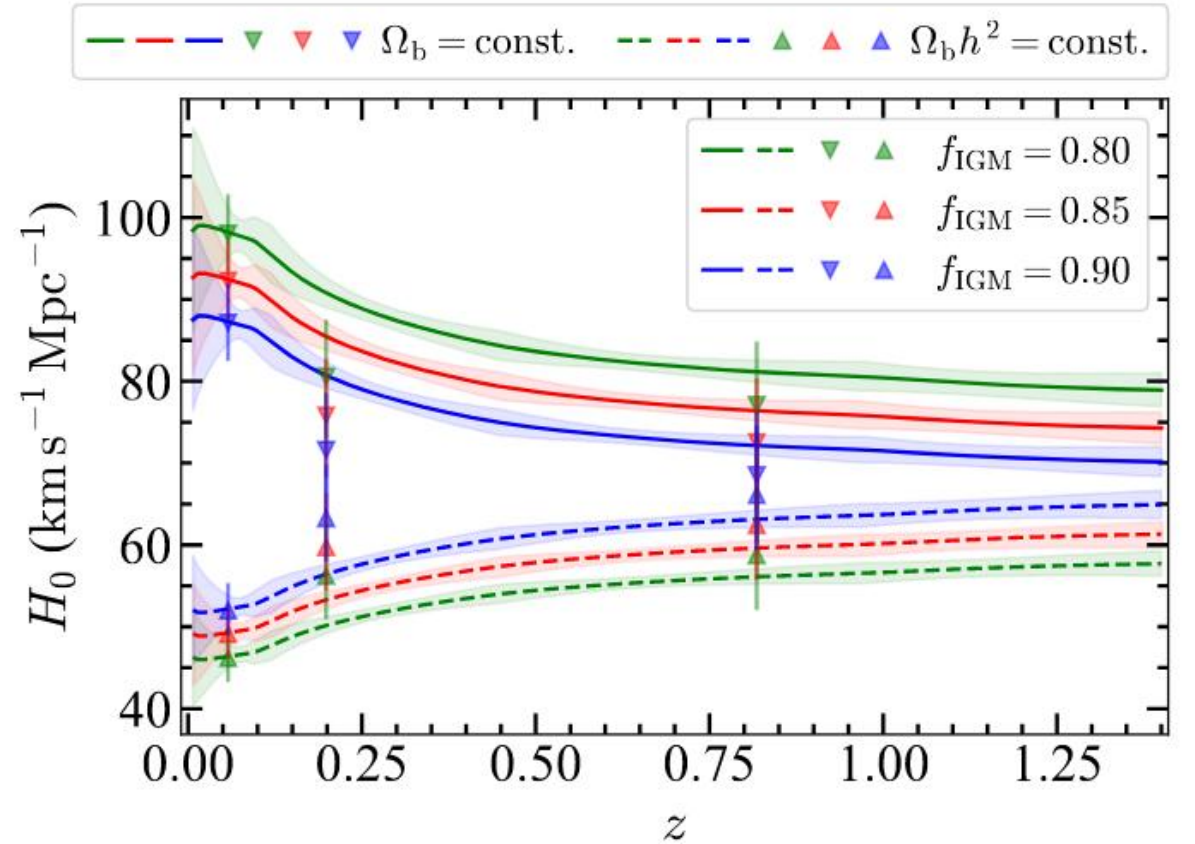


ML prediction shows  $DM' \approx 150 \text{ pc cm}^{-3}$  at  $z=0$ , corresponding to combined contribution from Galactic halo and host galaxy  $\Rightarrow DM_{\text{halo}} \approx 65, DM_{\text{host}} \approx 85$ .

## Initial Finding:

$$\langle \text{DM}_{\text{IGM}}(z_s) \rangle = \frac{3c\Omega_b H_0^2}{8\pi G m_p} \int_0^{z_s} \frac{f_{\text{IGM}}(z)\chi(z)(1+z)}{H(z)} dz$$

The inferred  $H_0$  was not a constant. It exhibited a systematic trend, evolving with redshift  $z$  (see solid lines in Fig.2).



## Key Method 2 - Bayesian Validation

### A Direct Test with a Bayesian Framework

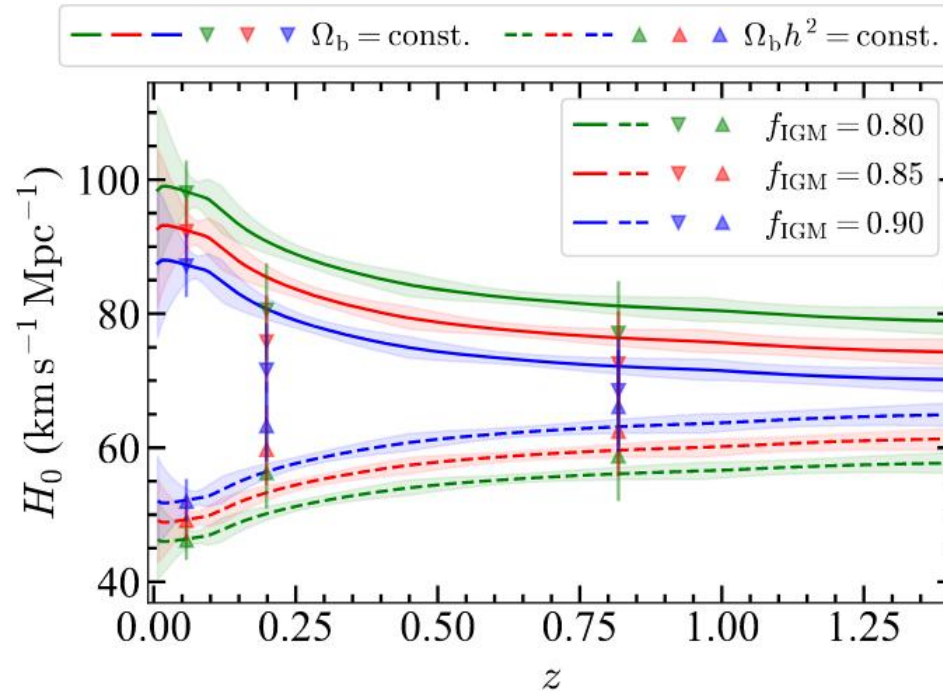
Data divided into 3 redshift bins

- Low-z: [0, 0.115], 36 samples
- Mid-z: [0.115, 0.282], 40 samples
- High-z: [0.282, 1.4], 38 samples

Independently estimate  $H_0$  in each bin ( $H_{01}$ ,  $H_{02}$ ,  $H_{03}$ )

$$\begin{aligned}\langle \text{DM}_{\text{IGM}}(z_s) \rangle &= \frac{3c\Omega_b H_{01}^2}{8\pi G m_p} \int_0^{z_1} \frac{f_{\text{IGM}}(z)\chi(z)(1+z)}{H_{01}\sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}} dz \\ &+ \frac{3c\Omega_b H_{02}^2}{8\pi G m_p} \int_{z_1}^{z_2} \frac{f_{\text{IGM}}(z)\chi(z)(1+z)}{H_{02}\sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}} dz \\ &+ \frac{3c\Omega_b H_{03}^2}{8\pi G m_p} \int_{z_2}^{z_s} \frac{f_{\text{IGM}}(z)\chi(z)(1+z)}{H_{03}\sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}} dz\end{aligned}$$

The Bayesian analysis strongly corroborated the ML findings. We again observed a statistically significant evolution of  $H_0$  across the different redshift bins (see scatter points in Fig. 2).



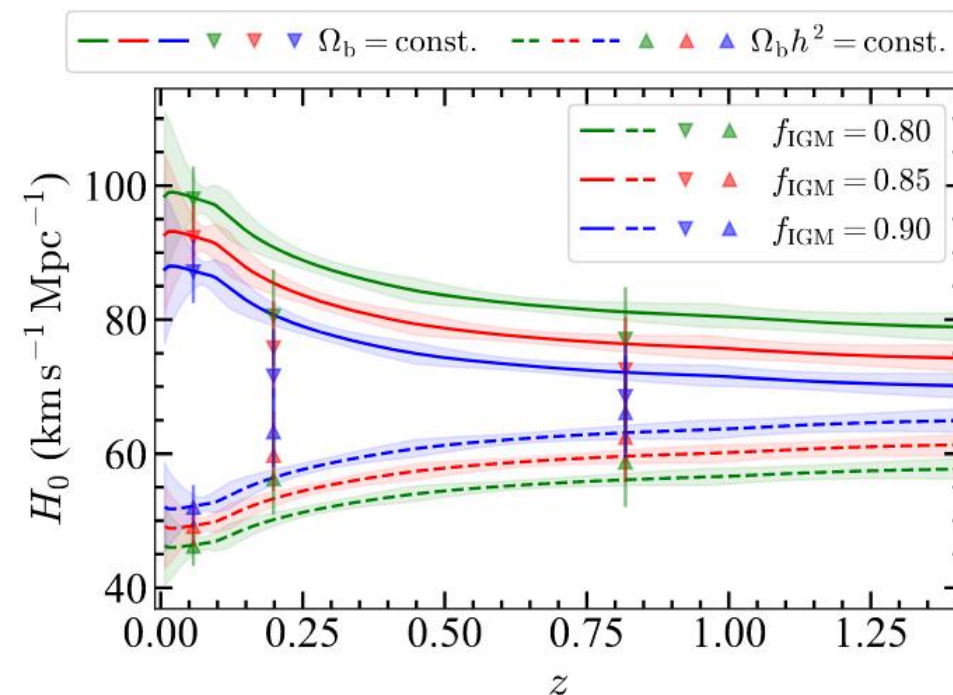
# Results

The Critical Result:  $H_0$  Varies Significantly with Redshift!

- When Fixing  $\Omega_b$ :  $H_0$  decreases with redshift
- When Fixing  $\Omega_b h^2$ :  $H_0$  increases with redshift
- Results robust across different  $f_{\text{IGM}}$  values (0.80, 0.85, 0.90)

**Two Methods Agree**

- ML continuous curves + Bayesian discrete points perfectly match
- → The core  $\Lambda$ CDM assumption (constant  $H_0$ ) is violated!





# Summary

- $\Lambda$ CDM is Inadequate: Standard cosmological model cannot explain the observed  $H_0$  redshift dependence
- New Interpretation of Hubble Tension: May not be observational errors, but a problem with the model itself
- Dark Energy May Be Dynamic: The cosmological constant  $\Lambda$  may be oversimplified.
- Further Test:  $w_0w_a$ CDM Model,  $H_0$  can remain constant within more flexible dark energy frameworks!



Thanks for your listening!

**Please feel free to contact us:**

kongjun.zhang@stu.ynu.edu.cn